

Optimal Power Flow Analysis of Interconnected Power System

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Abstract:

Electric utilities utilize various techniques to achieve optimal power flow. In this paper, linear programming method and Particle Swarm Optimization method is used for obtaining optimal power flow using equality and inequality constraints. To ensure secure operation of power system, it is necessary to keep the line flow within the prescribed MVA limits so that the system operates in normal state. With the involvement of nonlinear function and constraints, PSO method is more suitable than linear programming method.

This approach is examined and tested on standard IEEE 6 bus and 30 bus system. Test results of PSO is compared with linear programming method for different cases. The obtained solution proves that the proposed technique is efficient and accurate.

Keywords:

Optimal power flow; Linear Programming; Constraints; Particle Swarm Optimization; Security Constrained Economic Dispatch

I. Introduction

As the power industry moves into a more competitive environment, rigorous procedures for defining the level of inter-utility power exchanges are required. One of the available tools to evaluate power exchanges among utilities is the Optimal Power Flow (OPF). The use of an OPF is becoming increasingly important in solving the problem of inter-utility power transactions in deregulated electricity markets. Throughout the entire world, the electric power industry has undergone a considerable change in the past decade, and will continue to do so for the next several decades. In the past, the electric power industry has been either a government-controlled or a government-regulated industry which existed as a monopoly in its service region. All people, businesses, and industries were required to purchase their power from the local monopolistic power company. This was not only a legal requirement, but a physical engineering requirement as well. It just did not appear feasible to duplicate the resources required to connect everyone to the power grid [4]. Over the past decade, however, countries have begun to split up these monopolies in favour of the free market. The optimal power flow problem has been discussed since its introduction. Because the OPF is a very large, non-linear mathematical programming problem, it has taken decades to develop efficient algorithms for its solution. Many different mathematical techniques have been employed for its solution. The majority of the techniques discussed in the literature use one of the following five methods.

1. Lambda iteration method
2. Gradient method.
3. Newton's method
4. Linear programming method.
5. Interior point method.

The Linear Programming (LP) approach transforms the non-linear optimization problem into an iterative algorithm that in each iteration solves a linear optimization problem resulting from linearizing both the objective function and constraints. The large-scale application of LP-based methods has traditionally been limited to network constrained real and reactive dispatch calculations whose objectives are separable, comprising the sum of convex cost curves. The accuracy of calculation may be lost if the oversimplified approximation is adopted in LP-based OPF. The piecewise linear segmentation of the generator fuel cost curves should be good for avoiding this problem. The piecewise approach can fit an arbitrary curve convexly to any desired accuracy with a sufficient number of segments. Originally, a separable LP variable had to be used for each segment, with the resulting large problems with multiple segments cost curve modeling were prohibitively time and storage consuming [3]. Now days advancement in computing and parallel processing enables the population based search procedure like Genetic Algorithm, Evolutionary Programming and Particle Swarm Optimization to apply in the real time applications like OPF [2]. In this paper the Particle Swarm Optimization method is applied to solve Optimal Power Flow. The effectiveness of the proposed method is proved by applying it for a 6 bus and 30 bus system.

II. Overview

- **Linear programming method:**

Linear programming method is very adapt at handling constraints, as long as problem to be solved is linearized without loss of accuracy. In this technique nonlinear cost function of generator are linearized first. Those functions are divided into small parts as shown in figure.

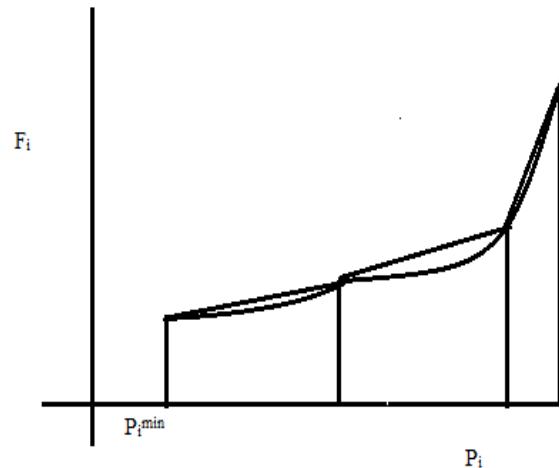


Fig.1: Linearization of cost curve

As shown in figure F_i is cost of that generator and P_i is the power produced by the generator. With the help of this linearization this method is used with ease [1].

- **Particle Swarm Optimization:**

The PSO is based on the researches on social behavior of organisms such as fish schooling and bird flocking provides a population-based search procedure in which individuals called particles change their positions (states) with time. While flying in a multi-dimensional search space, each particle adjusts its position with the new velocity which depends on its own experience (pbest) and the experience of neighboring particles (gbest),

i.e. making use of the best position encountered by itself and its neighbors. Let x and v denote a particle coordinates (position) and its corresponding flight speed (velocity) in a search space, respectively. The i^{th} particle is represented by,

$x_i = (x_{i1}, x_{i2}, \dots, x_{id})$ in the d -dimensional space.

The best previous position of the i^{th} particle is $pbest_i = (pbest_{i1}, pbest_{i2}, \dots, pbest_{id})$.

The index of the best particle among all particles in the group is represented by the $gbest$. The rate of the velocity for particle 'i' is represented as:

$v_i = (v_{i1}, v_{i2}, \dots, v_{id})$.

The modified velocity and position of each particle can be calculated using the current velocity and the distance from $pbest_{ij}$ and $gbest_j$ as shown in the following formulae:

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$$v_{ij}(t+1) = w(t) * v_{ij}(t) + c1 * rand() * (pbest_{ij} - x_{ij}(t)) + c2 * Rand() * (gbest_j - x_{ij}(t)) \quad (1)$$

$$x_{ij}(t+1) = x_{ij}(t) + v_{ij}(t+1) \quad (2)$$

$$i = 1, 2, \dots, n; j = 1, 2, \dots, d \quad (3)$$

where,

n - Number of particles in a population (Population size)

d - Number of variables in a particle - Iteration count

w - Inertia weight factor

$c1, c2$ - Acceleration constants

$rand(), Rand()$ - Uniform random value in the range [0,1]; $v(t)$ - Current velocity of particle at iteration, $v_{jmin} \leq v_j(t) \leq v_{jmax}$

$x(t)$ - Current position of particle at iteration.

In the above procedure, if the parameter v_{max} is too high, particles might fly past good solution. If v_{max} is too small, particles may not explore sufficiently beyond local solution. The constant c and c_2 represent the weighting of the stochastic acceleration terms that pull each particle toward the best and global best positions. Suitable selection of inertia weight $w(t)$ provides a balance between global and local explorations, thus requiring less iteration on average to find a sufficiently optimal solution, inertia weight is set according to the following equation.

$$w(t) = w_{max} - \{(w_{max} - w_{min}) / t_{max}\} * t \quad (4)$$

where t_{max} is the maximum number of iterations (generations) and 't' is the current number of iterations [5][6].

III. Problem formulation

• Linear programming method

The OPF problem is to optimize the steady state performance of power system in terms of an objective function while satisfying several equality and inequality constraints. Mathematically, the problem can be formulated as follows [5].

$$\text{Min } J(x) \quad (5)$$

$$\text{Subject to } g(x) = 0 \quad (6)$$

$$\text{And } h(x) \leq 0 \quad (7)$$

Now J is our objective function which is generator cost. J is minimized with respect to g . Objective function consists of f_x . Here x is active power of each generator.

Equality Constraints: Mostly generator power is optimized with this constraint. Here in this paper equality constraint is given by generated power should be equal to load and losses [4][1].

$$P_{gen} = P_{load} + P_{loss} \quad (8)$$

Inequality constraints: Generator power, line power, generator voltage can be optimized

with inequality constraints. Here in this paper inequality constraint is implemented by for any i^{th} line line flow f_i should not violate its maximum f_i^{max} and minimum f_i^{min} limits.

$$\min_i f_i \leq f_i \leq f_i^{max} \quad (9)$$

Hence with the help of inequality constraint line power limit is maintained.

Objective function: Objective function in linear programming is having control variables. Thus with the help of control variables objective function is optimized. Objective function in this paper is considered as the generator's operating cost and generator power is control variable. Hence generator's operating cost is to be reduced. This cost function can be optimized with the help of economical load dispatch. Objective function will be different for each particular generator. Here generalized function is shown

$$F_i(P_i) = a_i + b_i P_i + c_i P_i^2 \quad (10)$$

Here a_i, b_i, c_i are generator cost coefficients. These parameters are different for each generator.

• Particle Swarm Optimization

In the Optimal Power Flow with Line Flow Constraints, minimization of either the cost of generation or real power loss may be considered as objective function 'f'. The control variable 'u' may be taken as either a vector of real power generated or the generation voltage or both depends on the requirement. Mathematically, it can be formulated as,

$$\text{Min } f(x, u) \quad (11)$$

$$\text{subject to} \quad (12)$$

$$g(x) = 0 \quad (13)$$

$$P_{gmin}(i) \leq P_g(i) \leq P_{gmax}(i) \quad (14)$$

$$U_{min}(i) \leq U(i) \leq U_{max}(i) \quad (15)$$

$$S(i, j) \leq S_{max}(i, j) \quad (16)$$

The equations (13) to (16) represent the constraints on the power balance, maximum generation limit, system voltage limit and line flow limits respectively.

IV. Implementation

• **Linear programming method:**

The above mentioned method for solving optimal power uses an iterative technique to obtain the optimal solution, so it is also called a Successive Linear Programming (SLP) method. The solution procedure of SLP for optimal power flow are summarized below:

1. Select the set of initial control variables.
2. Solve the power flow problem to obtain base power for proposed system.
3. Prepare linear objective cost function and run linear programming to find power values.
4. Enter this power values in power flow and get new values of power (Power flow 1).
5. Check all generator values with its maximum and minimum values and if it's violated then set their limits.
6. Then select the new loss values of power flow and run LP.
7. Get LP-1 result and from that get new values of generator powers.
8. Put those values in objective cost function and check whether the cost is optimized or not.
9. Then check all the min and max limits of generator and line power and with the help of constraints.
10. Minimize the parameters ones who's out of max limits.

These steps are applied on our proposed system with the help of MATLAB programming. For calculating linear programming we need generator cost function in segments slopes. Its equation is

$$S_{ij} = F_i(P_i)^+ - F_i(P_i)^- \div (P^+ - P^-) \quad (7) \quad ij$$

• **Particle Swarm Optimization Algorithm**

Step 1: In OPF problem, each th particle is represented by $x_i = (x_{i1}, x_{i2}, \dots, x_{id})$, where 'x' consists of set of control variables 'u', Real power generation or voltage or both of all the units. Initialize randomly the individuals (particles) of initial population (the size of population matrix is $N \times D$) and velocities according to limits of each variable.

Step 2: To each individual of the population, run the load flow program to find the system voltages of dependent and controlled buses, real and reactive power generation of slack bus and controlled buses, MVA flows of transmission lines and total real power loss. The execution of load flow ensures to satisfy the constraint. Here, in this paper, full Newton method is used for its accuracy [7].

Step 3: For all the individuals, calculate the objective function value 'f' that maybe the total cost of generation or the total real power loss. For any individual, if any of the constraints specified by (6) to (8) is violated, add penalty to its objective function

Step 4: Each initial searching point is assigned as pbest of the individual and the best evaluated value among pbest's is set as gbest.

Step 5: Modify the velocity of each individual x_i according to (1). If any new velocity exceeds its limit set it at the limit.

Step 6: Modify the position of each individual according to (2). The modified values must satisfy the constraints on their limits.

Step 7: Find the objective function for the new position in the same way as initial positions (Steps 2 & 3).

Step 8: Compare each individual's objective function value with its pbest and if the objective function of the new position is less than previous pbest, assign the present position as pbest. The best evaluated value among pbest's is denoted as gbest.

Step 9: Repeat the step numbers 5 to 8 until the number of iterations reach the maximum.

Step 10: The latest value of gbest is the optimum solution that minimizes the objective function. [9]

V. Proposed system

Standard IEEE 6 bus and 30 bus system are used for approaching the proposed methods.

- IEEE 6 bus system:

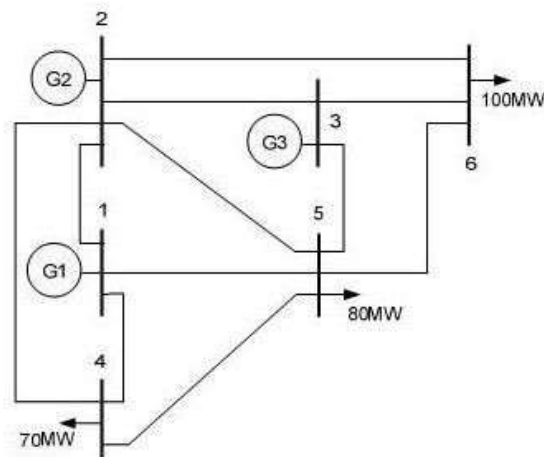
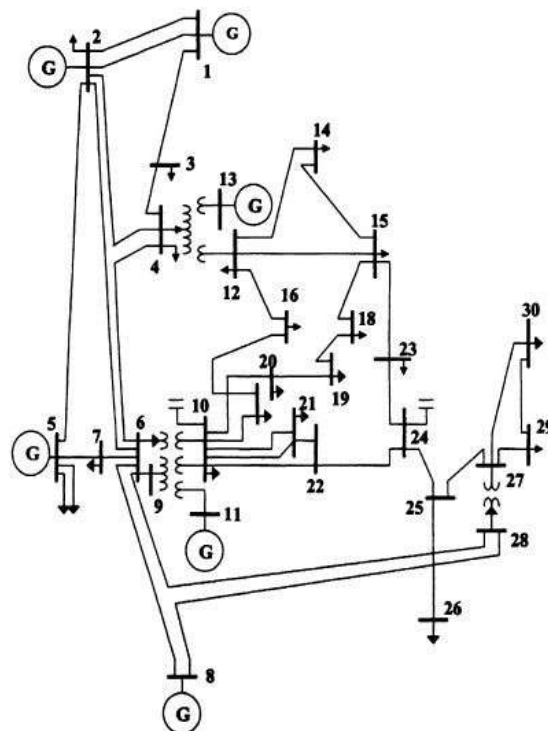


Fig.2:6Bussystem

In 6 bus system

3 generators are used to meet up demand. In that bus 1 is taken as slack bus. Total load for this system is 210 MW and losses are 8.57 MW.

- IEEE 30 bus system: Fig 3 shows 30 bus system [8]



As shown in fig 30 bus system consists of 6 generators. Total load for this system is 259.30 MW and losses are 17.59 MW. Bus 1 is taken as slack bus.

VI. Results And Discussion

The proposed algorithm of Particle swarm optimization is implemented on a 6 bus and 30 bus system and the results are compared with Linear Programming method.

Power output of three generators are considered as the control variable and OPF is executed to minimize the operating cost given by

n

$$f(u) = a_i P_{gi}^2 + b_i P_{gi} + c_i \quad (9), i=1 \text{ and } u = [P_{g1} P_{g3} \dots P_{gn}]$$

- Resultsof6bussystem:

3132
 3130
 3128
 3126
 3124
 3122
 3120

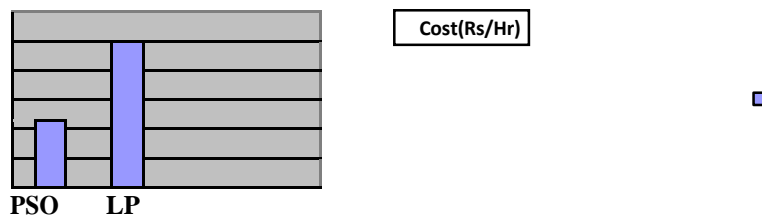


Fig4: Generator operating cost

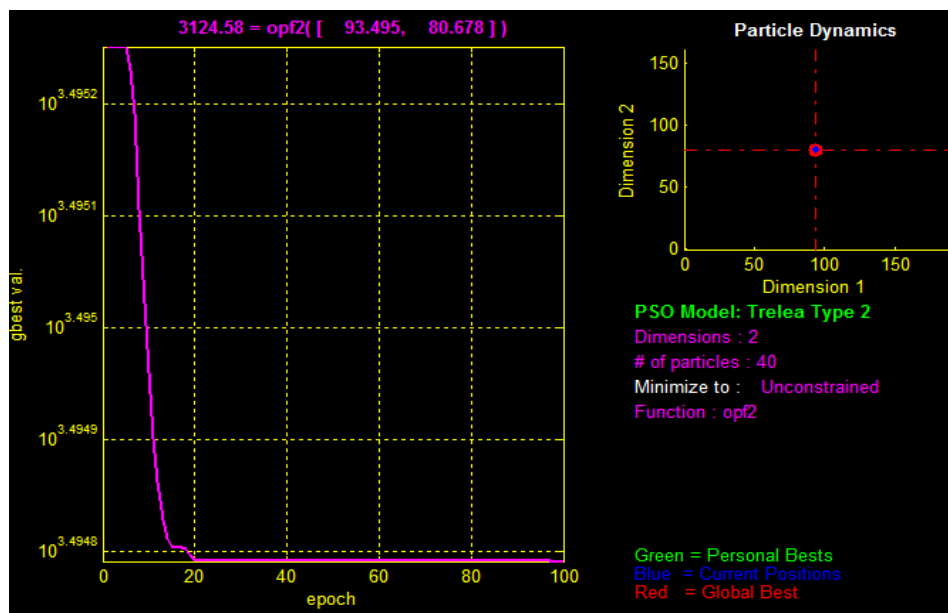
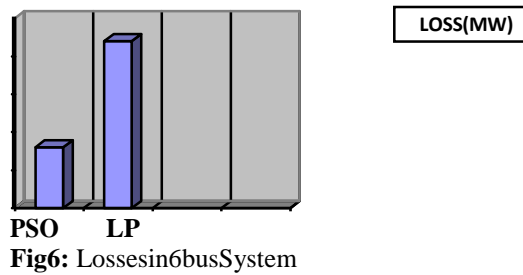


Fig5: Convergence characteristic of PSO for 6 bus system

6.9
 6.85
 6.8
 6.75
 6.7
 6.65



• Results of 30 bus system

3200
 3000
 2800
 2600
 2400
 2200

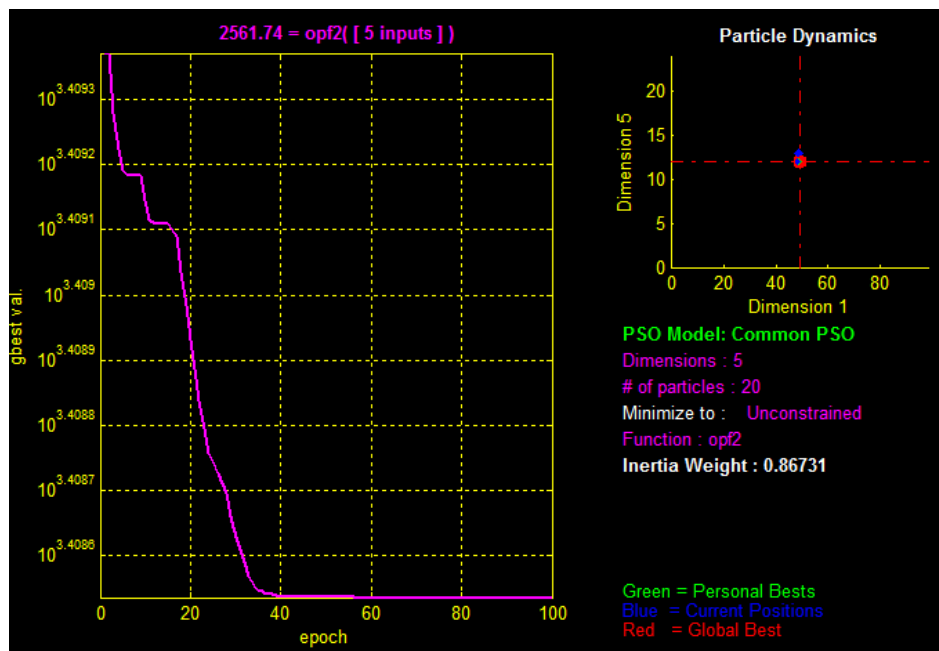
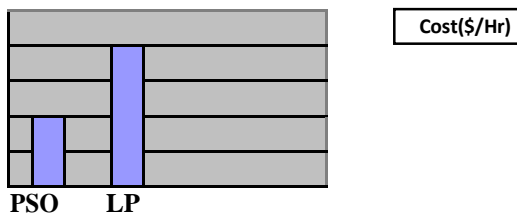


Fig.8: Convergence characteristic of PSO for 30 bus system

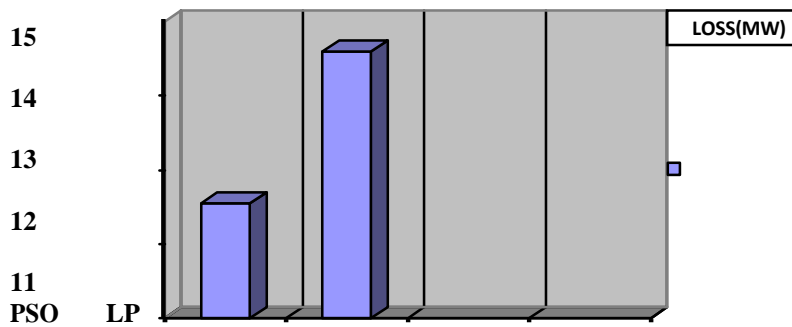


Fig9: Losses in 30 bus system

Above figures show that effectiveness of the proposed PSO approach compared to linear programming method as generating cost of generators are decreasing compared to linear programming method. As proposed approach PSO is implemented on both system total losses are also decreasing. Thus it is also seen that all the lines are within their MVA limits.

• **Parameter Selection:**

For the test system considered, the following PSO parameters are chosen after a trial and error process. $v_{max} = 10\%$ of x' ; $v_{min} = 0$; $w_{max} = 0.9$; $w_{min} = 0.4$; $c_1 = 2$; $c_2 = 2$; Population size = 24; Maximum number of iterations is found to be 100.

VII. Conclusion

Nowadays, as restructuring of power system increases the congestion of power flow in the transmission system, the Optimal Power Flow plays an important role in day-to-day power system operation and control to maintain system security. Particle Swarm Optimization technique is found to be highly suitable for Optimal Power Flow problem with line flow constraints. With the help of equality constraints and inequality constraints various parameters like generator power, line power, generator operating cost, reactive power can be optimized. It is also assured that the algorithm would function in the same way for large power systems with more number of lines and generating units. The computational results of the sample system reveal that the proposed method is much more efficient and versatile than other linear programming methods.

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Appendix

• **6busdata:**

Busdata

Busnumber	BusType	Voltage(pu)	Pgen. (pu)	Pload(pu)	Qload(pu)
1	1	1.05	-	-	-
2	2	1.05	0.50	0	0
3	2	1.07	0.60	0	0
4	0	0	0	0.7	0.7
5	0	0	0	0.7	0.7
6	0	0	0	0.7	0.7

Linedata

FromBus	To Bus	R(pu)	X(pu)	Shunt(pu)	Linelimit(MWA)
1	2	0.10	0.20	0.02	40
1	4	0.05	0.20	0.02	60
1	5	0.08	0.30	0.03	40
2	3	0.05	0.25	0.03	40
2	4	0.05	0.10	0.01	60
2	5	0.1	0.30	0.02	30
2	6	0.07	0.20	0.025	90
3	5	0.12	0.26	0.025	70
3	6	0.02	0.10	0.01	80
4	5	0.20	0.40	0.04	20
5	6	0.10	0.30	0.03	40

Generatorcostcoefficient

Generator	ai	bi	ci	PGmin(pu)	PGmax(pu)	Qmax (pu)
1	0.00533	11.669	213.1	50	200	-
2	0.00899	10.333	200	37.5	150	70
3	0.00741	10.833	240	45	180	70

• **30busdata**

Busdata

Bus no	Bustype	Voltage(pu)	Pgen(MW)	Pload(MW)	Qload(MW)
1	1	1.06	0	0	0
2	2	1.043	40	21.70	12.7
3	0	1	0	2.4	1.2
4	0	1.06	0	7.6	1.6
5	2	1.01	0	94.2	19
6	0	1	0	0	0
7	0	1	0	22.8	10.9
8	2	1.01	0	30	30
9	0	1	0	5.8	0
10	0	1	0	0	2
11	2	1.082	0	11.2	0
12	0	1	0	0	7.5
13	2	1.071	0	6.2	0

14	0	1	0	8.2	1.6
15	0	1	0	3.5	2.5
16	0	1	0	9	1.8
17	0	1	0	3.2	5.8
18	0	1	0	9.5	0.9
19	0	1	0	2.2	3.4
20	0	1	0	17.5	0.7
21	0	1	0	0	11.2
22	0	1	0	3.2	0
23	0	1	0	8.7	1.6
24	0	1	0	0	6.7
25	0	1	0	3.5	0
26	0	1	0	0	2.3
27	0	1	0	0	0
28	0	1	0	2.4	0
29	0	1	0	0	0.9
30	0	1	0	10.6	1.9

Linedata

FromBus	ToBus	R(pu)	X(pu)	Shunt(pu)	Linelimit(MVA)
1	2	0.0192	0.0575	0.02640	130
1	3	0.0452	0.1852	0.02040	130
2	4	0.0570	0.1737	0.01840	65
3	4	0.0132	0.0379	0.00420	130
2	5	0.0472	0.1983	0.02090	130
2	6	0.0581	0.1763	0.01870	65
4	6	0.0119	0.0414	0.00450	90
5	7	0.0460	0.1160	0.01020	70
6	7	0.0267	0.0820	0.00850	132
6	8	0.0120	0.0420	0.00450	20
6	9	0.0	0.2080	0.0	65
6	10	0	.5560	0	32
9	11	0	.2080	0	65
9	10	0	.1100	0	65
4	12	0	.2560	0	65
12	13	0	.1400	0	65
12	14	.1231	.2559	0	32
12	15	.0662	.1304	0	32
12	16	.0945	.1987	0	32
14	15	.2210	.1997	0	16
16	17	.0824	.1923	0	16
15	18	.1073	.2185	0	16
18	19	.0639	.1292	0	16
19	20	.0340	.0680	0	32
10	20	.0936	.2090	0	32
10	17	.0324	.0845	0	32
10	21	.0348	.0749	0	32
10	22	.0727	.1499	0	32
21	22	.0116	.0236	0	32

15	23	.1000	.2020	0	16
22	24	.1150	.1790	0	16
23	24	.1320	.2700	0	16
24	25	.1885	.3292	0	16
25	26	.2544	.3800	0	16
25	27	.1093	.2087	0	16
28	27	0	.3960	0	65
27	29	.2198	.4153	0	16
27	30	.3202	.6027	0	16
29	30	.2399	.4533	0	16
8	28	.0636	.2000	0.0214	32
6	28	.0169	.0599	0.065	32

Generator cost coefficient

Generator	a_i	b_i	c_i	PGmin(pu)	PGmax(pu)	Qmax(pu)
1	0.00375	2	0	50	200	-
2	0.0175	1.75	0	20	80	-
3	0.0625	1	0	15	50	-
4	0.0083	3.25	0	10	35	-
5	0.025	3	0	10	30	-
6	0.025	3	0	12	40	-